## Prospects for lattice field theory beyond the standard model

#### Georg Bergner Friedrich Schiller University Jena





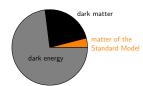


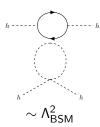


Lattice 2024: Aug 3, 2024

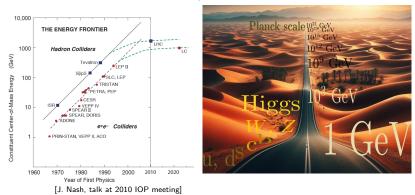
#### Shortcomings of the standard model

- missing pieces of the standard model
  - explanation for dark matter/dark energy
  - gravitational interactions
  - neutrino masses . . .
- aesthetic imperfection of the standard model
  - parametrization or explanation
  - hierarchy problem
  - missing unification or symmetry
  - flavor hierarchy
- missing understanding
  - confinement mechanism
  - quantum gravity
  - gauge/gravity duality





#### What can be expected from colliders?



- speed is slowing down and will stop eventually
- but there might be an oasis just a few miles away
- ...or it just means a free way to quantum gravity

## Where is new physics hiding?

Our current BSM collider discoveries are constraints.

Directions for new observations:

- energy
- precision
- cosmology
- from on-shell to off-shell discoveries

Solution to SM problems without constraint violation:

- small coupling to the Standard Model
- large suppression of  $\frac{1}{\Lambda_{BSM}}$
- large gap to new physics

#### Important contributions required from the lattice

- precision input for QCD contributions:
  - new routes towards detection
  - QCD-corrections to observed anomalies
  - $\rightarrow$  not covered in this talk
- test of BSM strong interactions, goals at different levels
  - test specific models to add constraints like an experiment
  - fundamental concepts behind the suggested models
  - theory space of strong interactions relevant for model building and our general understanding

interplay with conceptual questions about strong interactions

#### BSM concept: Supersymmetry

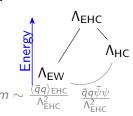
- original motivation for SUSY BSM: hierarchy problem solution by symmetry: boson-fermion cancellation
- needs unknown (non-perturbative) breaking mechanism
- heavily investigated regarding BSM and collider signatures (MSSM etc.)
- dark matter: standard WIMP scenario
- general concepts with may applications: gauge/gravity duality etc.

## Shifted perspective of SUSY applications:

supersymmetric gauge theories  $\leftrightarrow$  analytic predictions, dualities

#### BSM concept: Composite Higgs/ technicolor

- solve hierarchy problem by new strong interactions [S. Weinberg (1976)]
- naturally leads bound states as possible dark matter
- generate fermion masses from effective operators of extended hyper color theory
- constraints:
  - need bound state Higgs much lighter than other bound states
  - FCNC need to be suppressed
  - electroweak precision data

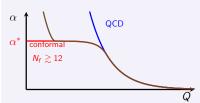


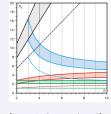
## BSM concept: Composite Higgs/ technicolor scenarios

#### Walking scenario

$$\beta(g) = -\frac{1}{(4\pi)^2} \left( \frac{11N_c}{3} - \frac{4}{3} T_R N_f \right) g^2 - \beta_1 g^5 + \dots$$

- ullet conformal window:  $N_{f,L} < N_f < N_{f,U}$  [T. Banks, A. Zaks (1981)]
- near conformal running enhances condensate over FCNC  $\langle \bar{q}q \rangle_{EHC} \sim \left( \frac{\Lambda_{EHC}}{\Lambda_{HC}} \right)^{\gamma_m} \langle \bar{q}q \rangle_{HC}, \gamma_m \text{ large}$  [T. Appelquist et al. (1987), Yamawaki et al. (1986)]
- light scalar, possibly dilaton-like





[Dietrich, Sannino (2007)]

## BSM concept: Composite Higgs scenarios

#### Walking scenario

#### Higgs from scalar pNGb

- spontaneous symmetry breaking generates light Higgs
   [D. B. Kaplan, H. Georgi (1984)]
- requirements for chiral symmetry group, e. g. by  $SU(2N_c) \rightarrow Sp(2N_c)$  (pseudoreal)
- HC chiral symmetry breaking preserves  $G_{SM} = SU(2)_L \times U(1)$
- scalar field generated at  $\Lambda_{NC}$  gets lower scale vev. v (EW breaking scale)

## BSM concept: Composite Higgs scenarios

#### Walking scenario

#### Higgs from scalar pNGb

#### Partial compositeness [Kaplan (1991)]

- need to generated vastly different fermion masses
- large top mass generated by coupling with fermion bound state  $\lambda \bar{\psi} B$
- UV theories classified according to symmetries [G. Ferretti, D. Karateev (2013)]
- 3 fermion operator (B) needs enhancement: combine with walking ? [v. Ayyar et al. (2018), A. Hasenfratz et al. (2023)]

## BSM concept: Strongly interacting dark matter

bound state of strong interactions: glueball, meson, baryon, gluino-glue...

- dark matter needs to be stable, but can cover large mass range
- not visible by current direct detection
- astronomical observations limit self interaction, hints for small non-vanishing self interactions
- relic abundance,  $\rho_{DM} = 5\rho_{baryon}$ :
  - thermal freeze-out dark matter, e. g. WIMP and SIMP
  - SIMP: 3→2 process by Wess-Zumino-Witten term
     [Y. Hochberg et al. (2014)]
  - asymmetric dark matter
  - ...
- first order transitions lead to gravitational wave signatures in early universe

#### Other BSM concepts

Not covered in detail, though investigated on the lattice

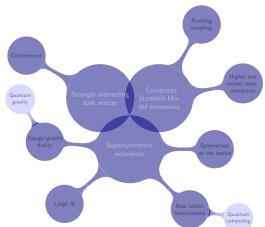
- symmetric mass generation (see talk by David Tong (Wed), S. Catterall (Fri))
- scalar gauge theories (talk by G. Catumba (Fri) on 2HDM, poster by E. Carstensen)
- QCD Axions, closely related to QCD-vacuum structure (talk by J. J. Hernández (Mo), many related talks)
- Hosotani mechanism
- extra dimensions
- quantum gravity
- . . .

## Beyond model building: BSM to extend our understanding

 standard model extension introduce new concepts

 challenge our knowledge of strong interactions

 provide new analytic approaches due to symmetries/properties of BSM strong interactions



#### Topics considered in this talk

- composite dark matter SU(4) (hyper) stealth dark matter Sp(4)  $N_f = 2$  as SIMP candidate
- composite Higgs and walking/conformal behavior Sp(4)  $N_f = 2 + N_{f,AS} = 3$  antisymmetric: partial compositness SU(3)  $N_f = 8$  near conformal and SMG SU(2)  $N_f = 1$  adjoint QCD
- progress of supersymmetric theories supersymmetric gauge theories in 4d gauge-gravity duality in lower dimensions

#### Hiding dark matter from direct detection

#### Some basic considerations:

- stable dark matter bound state:
  - ⇒ baryonic bound state
- neutrality by confinement: larger interactions at higher energies in early universe
- avoid leading electromagnetic interactions:
  - $\Rightarrow$  scalar baryons (even  $N_c > 2$ )
- meson decay, but no conflict with ew precision data:
  - ⇒ small Higgs coupling
- coupling to the standard model only by polarizability and Higgs boson exchange highly suppressed

Hidden, but still close to detection.

#### Stealth dark matter models

Stealth dark matter: SU(4),  $N_f=4$  [T. Appelquist et al. [LSD] (2015)]

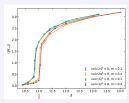
- direct detection limits: em polarizability [T. Appelquist et al. (2015)] and Higgs coupling [T. Appelquist et al. (2014)]
- $M_{DM} > 0.2 \text{ TeV}$
- bound state masses [T. Appelquist et al. (2014)] and towards baryon scattering [R. C. Brower et al. 2023]
- gravitational wave signatures from phase transition [R. C. Brower et
   al.2021]
- important difficult challenge: self interactions

Hyper stealth dark matter [V. Ayyar [LSD] arXiv:2402.07362]

- SU(4)  $N_f = 1$  light (plus heavy flavors)
- no light pNGbs, less detection constraints
- light flavor with possible tiny electroweak coupling ( $\eta'$  decay)
- ullet lowest possible mass in this framework:  $M_{DM}\sim {
  m few}~{
  m GeV}$

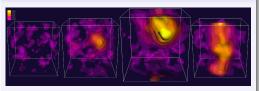
#### Gravitational wave signals from first order transition

Phase transitions of hyper stealth dark Density of states in finite matter [Talk by S. Park (Fri)]



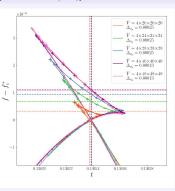
Domain-Wall fermions. signature of 1st order confinement trans.

Resolving the critical bubble in Yang-Mills theory [poster R. Seppä, talk D. Weir (Mon)]



temperature Sp(4)

[Talk D. Mason (Wed)]



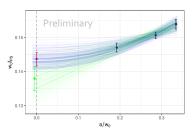
## SU(2) gauge theory, dark matter and composite Higgs

SU(2) gauge theory with  $N_f = 2$  fundamental flavors:

- dark matter with SIMP scenario
- composite Higgs theory: scalar pNGBs
- can be extended to walking technicolor by adding adjoint fermions [T. A. Ryttov, F. Sannino (2008)] [GB, S. Piemonte (2021)]
- lattice studies:
  - particle spectrum
  - scattering and self interactions
  - ...

Talk by L. S. Bowes and S. Martins (Fri):

- exp. clover Fermion action
- target smaller fermion masses for singlet meson decay:  $m_{\sigma} < 2m_{ps}$



## Sp(4) gauge theories as composite Higgs and dark matter

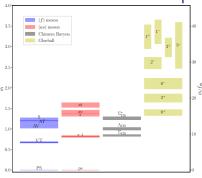
- $SU(2N_f) \rightarrow Sp(2N_f)$  chiral symmetry breaking for  $Sp(2N_c)$  theory: scalar pNGbs
- $N_f = 2 + N_{f,AS} = 3$  allows for partial compositeness
- SU(2) = Sp(2),  $N_f = 2$  simplest example with Wess-Zumino-Witten term (SIMP dark matter)
- Sp(4),  $N_f = 2$  next complicated choice
- larger N<sub>c</sub> might provide a larger parameter range for SIMP
   [M. Hansen et al. (2016)]

## Lattice investigations of Sp(4)

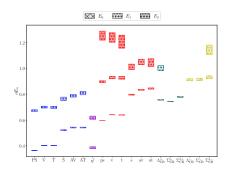
#### Recent investigations

- scan of theory space: quenched meson and glueball spectroscopy in the large  $N_c$  limit  ${\rm Sp}(2N_c)$  for  $N_c=2,3,4$  [E. Bennett et al. (2023)]
- analysis of the top partner (chimera baryon)
- dynamical  $N_f = 2 + N_{f,AS} = 3$  meson and glueball spectroscopy
- N<sub>f</sub> = 2 dark matter self interaction (meson scattering) provides lower bound of dark pion mass: 100 MeV
   [Y. Dengler et al. (2024)]
- important missing information for partial compositeness: anomalous dimension of chimera baryon
  (see SU(4) partial compositeness model [V. Ayyar et al. (2018), A. Hasenfratz et al. (2023)])

## Particle spectrum of Sp(4)



[E. Bennett et al. Phys.Rev.D 109 (2024)] massless continuum limit from quenched simulations gradient flow units



[E. Bennett et al. (2024)] single ensemble, in lattice units

Spectroscopy using spectral densities (see Talk by H. Hsiao Fri) Further results: flavor singlet mesons (Talk by F. Zierler, Tue)

## Considerations of walking scenario and conformal window

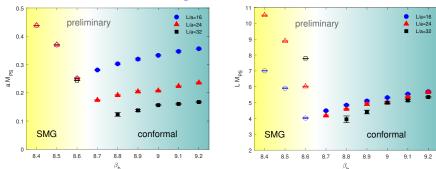
- landscape of gauge theories with gauge group G,  $N_f$  fermions possible in multiple representations
- conjectured IR behavior has to be confirmed with lattice data
- methods:
  - scaling of particle spectrum
  - Schrödinger functional
  - gradient flow
  - mode number
  - . . .
- conformal: scaling of masses  $M_H \sim m^{1/\gamma_m}$
- requires also control of phase transition, topology, etc.

## SU(3) with $N_f = 8$ possible edge of conformal window

Indications for a rich phase space with staggered fermions [A. Hasenfratz PRD 106 (2022)]

- no clear signal from running coupling, but observation of two phases
- weak coupling phase: looks conformal
- strong coupling: SMG chiral symmetric, confining
- Pauli-Villars fields to avoid bulk transitions

# SU(3) with $N_f = 8$ walking theory and symmetric mass generation



- SMG phase: mass gap independent from volume
- conformal phase: mass scaling given by the volume

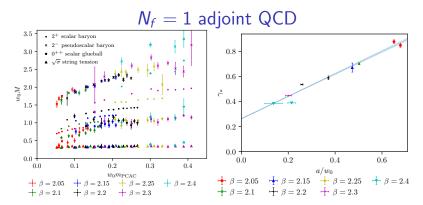
see talks by A. Hasenfratz, O. Witzel

# Conformal window for fermions in the adjoint representation

- hard to determine conformal window: limited range of scales on the lattice, mass deformations
- SU(3)  $N_f$  fundamental: large number of investigations
- motivation for considering adjoint rep.: lower  $N_{f,L}$  might be better for pheno.
- adjoint representation:  $N_f=2$  investigated as MWT seems to be inside conformal window [S. Catterall, F. Sannino (2007), L. Del Debbio et al. (2010)...] like also  $N_f=3/2$  [GB et al. (2018)]

 $N_f=1$  very challenging, new data [A. Athenodorou et el. (2024)]:

- large volumes with Wilson fermions
- large coupling range
- smallest possible masses



- conformal-like: light scalar
- neither agreement with conformal scaling, nor with chiral perturbation theory
- $\gamma^*$  from mode number shows  $\beta$  dependence poster by E. Bennett: improved strategies for further investigations

#### Tensions and systematics

EFT powerful framework, how to extend to walking case?

- recent new investigations of relations between different approaches [M. Golterman, Y. Shamir (2024)]
- dilaton EFT and soft theorems: R. Zwicky (Tue)

#### Other general questions:

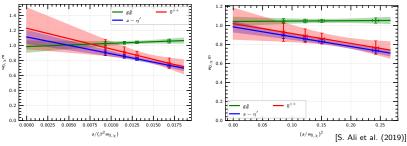
- How to think about lattice artefacts and scaling corrections?
- What kind of additional fixed points might be induced?
- Why is there such a light scalar in the theories with adjoint fermions?
- How large can anomalous dimensions be in practice?

#### Supersymmetry on the lattice

Supersymmetry on the lattice can only be fine-tuned or accidental

- Short explanation:  $\left\{ \mathbf{Q} , \mathbf{\bar{Q}} \right\} \sim \gamma^{\mu} \mathbf{P}_{\mu}$ , but space-time symmetries are broken
- long explanation: conflict between locality and symmetry (like chiral symmetry), but no Ginsparg-Wilson solution
- accidental:
  - $\mathcal{N}=1$  supersymmetric Yang-Mills theory: chiral symmetry  $\leftrightarrow$  SUSY  $\mathcal{N}=4$  supersymmetric Yang-Mills theory: subset of SUSY  $\leftrightarrow$  full SUSY
- lower dimensional theories allow alternative solutions

## Supersymmetric gauge theories in four dimensions



- $oldsymbol{ iny } \mathcal{N}=1$  supersymmetric Yang-Mills theory: SUSY recovered on the lattice
- non-perturbative properties like phase transitions and condensate determined on the lattice
- towards SQCD (tuning of O(10) counterterms): talk by H. Herodotou (Tue)

## New twists to $\mathcal{N}=1$ supersymmetric Yang-Mills theory

#### Gluino condensate in SYM:

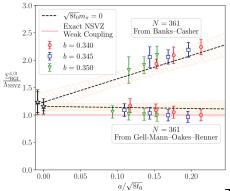
$$\Sigma = \begin{cases} 2e\Lambda^3/N & \text{strong coupling [G. C. Rossi, G. Veneziano (1984)]} \\ \Lambda^3 & \text{weak coupling [V. A. Novikov et al. (1984)]} \\ N\Lambda^3 & \text{twisted bc [M. Anber, E. Poppitz (2023)]} \end{cases}$$

- analytically calculable, but three different results are obtained
- previous studies of the condensate: Domain-Wall fermions:
   [J. Giedt et al. (2009)]; overlap and gradient flow [GB et al. (2019)][S. Piemonte, GB (2020)]

#### $\mathcal{N}=1$ SYM on the lattice: the chiral condensate

 new simulations based on twisted twisted Eguchi-Kawai: lattice formulation of large N SYM with Wilson fermions

[A. Gonzalez-Arroyo, M. Okawa (2013)]



#### Methods:

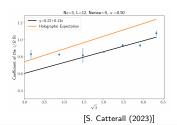
- 1) mode number from lowest eigenmodes of Wilson-Dirac
- 2) GMOR relation

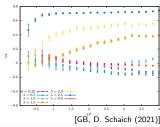
 $N_c$  dependence as predicted by weak coupling result [C. Bonnano et al. (2024)]

Talk by C. Bonnano (Mon)

## $\mathcal{N}=4$ supersymmetric Yang-Mills theory

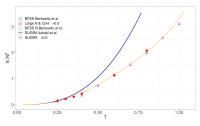
- combining the space-time and *R* symmetries to preserve one SUSY on the lattice, recover 15 SUSY in continuum limit
- main obstacle has been overcome: simulations have reached larger couplings [S. Catterall (2023)]
- promising first data indicates correctness of the method, waiting for coming investigations
- interesting: RG flow with conformal theory





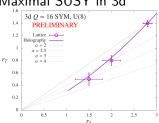
## Supersymmetry and gauge/gravity duality

- towards quantum gravity on the lattice
- evidence for gauge/gravity duality conjectures



[S. Pateloudis et al. [MCSMC] (2023)]

## Poster by D. Schaich: Maximal SUSY in 3d



 $r_L^2 \times r_T$  torus, critical  $T_c$ 

#### Conclusions

- long standing problem, how to fix the standard model might still require new solutions
- like collider experiment: quite mature developments for BSM strong interactions can be further constrained by lattice simulations
- after years of investigations: still surprised and puzzles in the landscape of strongly interacting theories
- BSM leads to new perspectives on strong interactions
- interesting interplay to theoretical developments like gauge/gravity duality

Thanks for all the contributions, discussions, and input material. Unfortunately not all could be covered in this talk.